

Economic Frictions and Heterogeneous Impact of Net Worth Shocks

Cheng Ding, Tianhao Zhao

Department of Economics
Emory University

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Introduction

- The wealth effect is a critical channel through which economic shocks propagate: and [Mian, Rao and Sufi \(2013\)](#); [Mian and Sufi \(2014\)](#) proposed **net worth shock** and the household balance sheet channel
- The presence of financial and nominal frictions can amplify the effects of net worth shocks and impede the recovery process
 - Financial friction: Collateral constraint
 - Nominal friction: Downward Nominal Wage Rigidity (DNWR)
- **This paper:**
 - Develops a tractable two-agent model to illustrate the how the interaction between the two frictions leads to non-linear heterogeneous impacts of net worth shock
 - Builds a novel county-level dataset (*CountyPlus*)
 - Empirically estimates and does inference on the non-linear heterogeneous effects using semi-varying coefficient local projections

Introduction

Related studies:

- Net worth shock and slow recovery: Mian, Rao and Sufi (2013); Mian and Sufi (2014); Bocola and Lorenzoni (2020); Guerrieri, Lorenzoni and Prato (2020); Greg Kaplan, Kurt Mitman and Giovanni L. Violante (2020); Greg Kaplan, Kurt Mitman and Giovanni L. Violante (2020) ...
- Financial, nominal frictions and their impact: Christiano, Eichenbaum and Trabandt (2015); Schmitt-Grohé and Uribe (2016); Shen and Yang (2018) ...

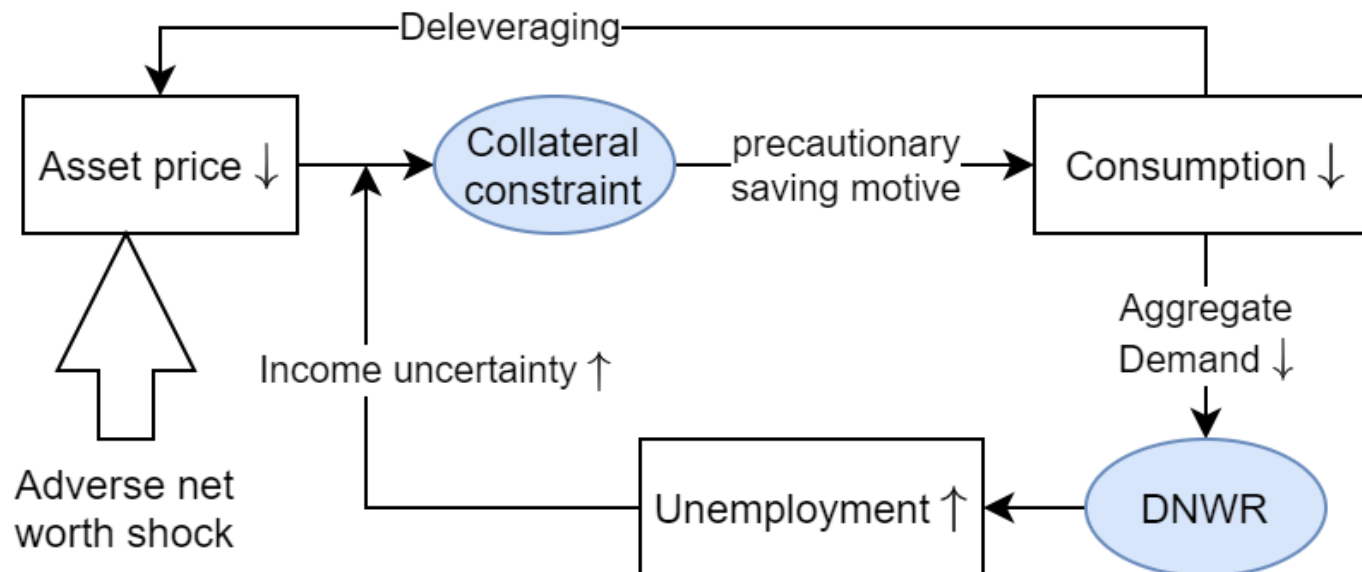
Methodology:

- Local projections (LP) and heterogeneous effect estimation: Jordà (2005); Jordà, Schularick and Taylor (2020); Cloyne, Jordà and Taylor (2023) ...
- Estimation and inference of semi-varying coefficient model: Fan, Zhang and Zhang (2001); Zhang, Lee and Song (2002); Fan and Huang (2005); Hu (2024) ...

Introduction

Key findings:

- Mechanism: adverse net worth shock \rightarrow higher precautionary savings and deleverage in response to tightened collateral constraints. DNWR \rightarrow higher income uncertainty. The adjustment process is prolonged, leading to a persistent decline in consumption.
- Found significant heterogeneity in the impact of net worth shocks across counties, with the effect magnitude varying by the degree of local financial and nominal frictions.
- Suggested that the impact of net worth shocks can be non-linearly amplified when both collateral constraints and DNWR are binding.



Introduction

Key findings:

- Mechanism: adverse net worth shock \rightarrow higher precautionary savings and deleverage in response to tightened collateral constraints. DNWR \rightarrow higher income uncertainty. The adjustment process is prolonged, leading to a persistent decline in consumption.
- Found significant heterogeneity in the impact of net worth shocks across counties, with the effect magnitude varying by the degree of local financial and nominal frictions.
- Suggested that the impact of net worth shocks can be non-linearly amplified when both collateral constraints and DNWR are binding.

Main contributions:

- Adds empirical evidence of how financial and nominal frictions affect the impact of net worth shocks.
- Proposes a tractable model to illustrate the amplification mechanism of the frictions.

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A tractable two-agent model

- $t = 0, 1, 2, \dots$, economy's state s^t , and aggregate housing productivity shock $u(s^t)$
- Two assets:
 - Housing wealth $h(s^t)$ of price $p(s^t)$
 - State-contingent claims $b(s^{t+1})$ of price $q(s^{t+1}|s^t)$
- Two agents:
 - **Expert**: risk-averse on consumption; produce consumption goods using their housing wealth $h(s^t)$ and household's labor $l(s^t)$; borrow state-contingent claims
 - **Household**: risk-neutral on consumption and risk-averse on housing; constantly supply 1 unit of labor; save in the state-contingent claims
- Two frictions:
 - Collateral constraint: Experts face $b(s^{t+1}) \leq \theta p(s^{t+1})h(s^t), \forall s^{t+1}$
 - DNWR: $w(s^t) \geq \delta w(s^{t-1})$ and $(1 - l(s^t))(w(s^t) - \delta w(s^{t-1})) = 0$
- The collateral constraint prevents experts from very large amount of borrowing \implies **not** complete market

A tractable two-agent model

Expert's problem

$$V^b(s^t) = \max_{c(s^t), \{b(s^{t+1})\}, h(s^t), l(s^t)} \log c(s^t) + \beta \mathbb{E} V^b(s^{t+1})$$

$$c(s^t) + p(s^t)h(s^t) = n(s^t) + \sum_{s^{t+1}} q(s^{t+1} | s^t) b(s^{t+1}) \quad (\text{Budget})$$

$$n(s^t) := p(s^t)h(s^{t-1}) + y(s^t) - b(s^t) \quad (\text{Net worth})$$

$$y(s^t) := Y(s^t) - w(s^t)l(s^t) \quad (\text{Profit})$$

$$b(s^{t+1}) \leq \theta p(s^{t+1})h(s^t), \forall s^{t+1} \quad (\text{CC})$$

where

- $n(s^t) \geq 0$: net worth
- $Y(s^t) := Al^\alpha(s^t)[u(s^t)h(s^t)]^{\{1-\alpha\}}$

A tractable two-agent model

Household's problem

$$V^l(s^t) = \max_{c^l(s^t), \{a(s^{t+1})\}, h^l(s^t)} c^l(s^t) + \gamma \log h^l(s^t) + \beta \mathbb{E}V^l(s^{t+1})$$

$$c^l + \sum_{s^{t+1}} q(s^{t+1} | s^t) a(s^{t+1}) + p(s^t) [h^l(s^t) - h^l(s^{t-1})] = w(s^t) l(s^t) + a(s^t)$$

Housing market

$$h(s^t) + h^l(s^t) = H, H \in \mathbb{R}$$

Bond market

$$a(s^{t+1}) = b(s^{t+1}), \forall s^{t+1}$$

DNWR conditions

$$w(s^t) \geq \delta w(s^{t-1})$$

$$[1 - l(s^t)][w(s^t) - \delta w(s^{t-1})] = 0$$

A tractable two-agent model

Scenario (one-shot deviation)

1. $t = 0$: Unbinding deterministic steady state
2. $t = 1$: u_1 drawn from a distribution over support $(0, \bar{u}]$
3. $t \geq 2$: The realized path of $\{u_t\}$ is always 1

Then,

- Solve the equilibrium of one-shot deviation analytically
- Prove: persistent effects of u_1 shock
- Prove: non-linear heterogeneous impact of u_1

A tractable two-agent model

Proposition (Persistent Effect)

There exist a unique continuation equilibrium that depends on the states

$$(u_1, h_0, b_1(u_1))$$

In the continuation equilibrium, the collateral constraint is binding for a finite number of periods J , with $J = 0$ if $n_1(u_1) \geq \bar{n}_1 := \bar{p}\bar{h}^{\frac{1-\beta\theta}{\beta}}$, where \bar{p} and \bar{h} are jointly determined by

$$(1 - \beta)\bar{p} = \frac{\gamma}{H - \bar{h}}$$

$$\bar{p}(1 - \beta) = \beta(1 - \alpha)\bar{h}^{-\alpha}$$

A tractable two-agent model

Proposition (Non-linear heterogenous effect)

There exist levels of the entrepreneur's financial friction parameter θ and the DNWR parameter δ , such that if

$$\frac{w_0}{n_0} \geq \frac{\alpha}{\delta(1-\alpha)} \left[1 + (1-\theta)(1-\alpha) \left(\frac{p_0 h_0^l}{\gamma} - 1 \right) \right]$$

then, in equilibrium, the $t = 1$ collateral constraint and DNWR both bind when u_1 is in a non-empty interval $[\hat{u}_{\text{lb}}(\theta, \delta), \hat{u}_{\text{up}}(\theta, \delta)]$. In this case, the u_1 shock effects:

$$\frac{\partial c_1}{\partial u_1} > 0, \quad \frac{\partial l_1}{\partial u_1} > 0, \quad \frac{\partial p_1}{\partial u_1} > 0 \text{ or } < 0 \text{ or } = 0 \text{ depends}$$

in which these effects are also non-linear functions of θ and δ .

A tractable two-agent model

Comparative statistics

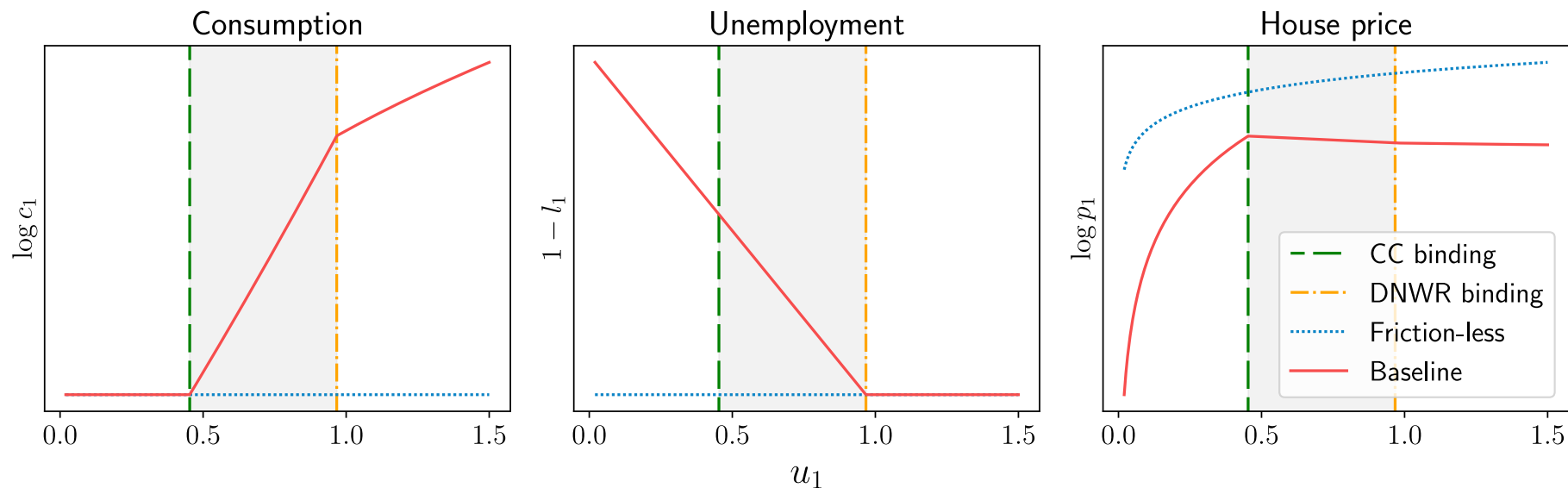


Figure 2: baseline vs. friction-less economy

where:

- Collateral constraint binds when $u_1 \geq$ Green line
- DNWR binds when $u_1 \leq$ Orange line
- Both binds: Grey area

\Rightarrow Amplification effects

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Data: CountyPlus

- Build a new open-source panel data set *CountyPlus*
 - 03-19 yearly, 3058 US counties
 - Fully replicable: 20+ public available data sources
 - Github: github.com/Clpr/CountyPlus
- Covers: household balance sheet by asset; income and consumption; labor and housing market indicators; friction measures; demographics; ...
- Key variables:
 - Household net worth (wealth)
 - Consumption, unemployment and house price
 - **DENI**: home mortgage denial due to lack of collateral / total denials
 - **FWCP**: Fraction of Wage Cuts Prevented
- Net worth shock is identified as:

$$x_{i,t} := \sum_{j \in \{S, B, H\}} s_{i,t-1}^j g_{t-1,t}^j$$

where i is county, S is equity, B is bond, H is housing wealth; $s_{i,t-1}^j$ is lag asset share in the balance sheet; and $g_{t-1,t}^j$ is the lag aggregate growth of asset prices.

Definition: net worth

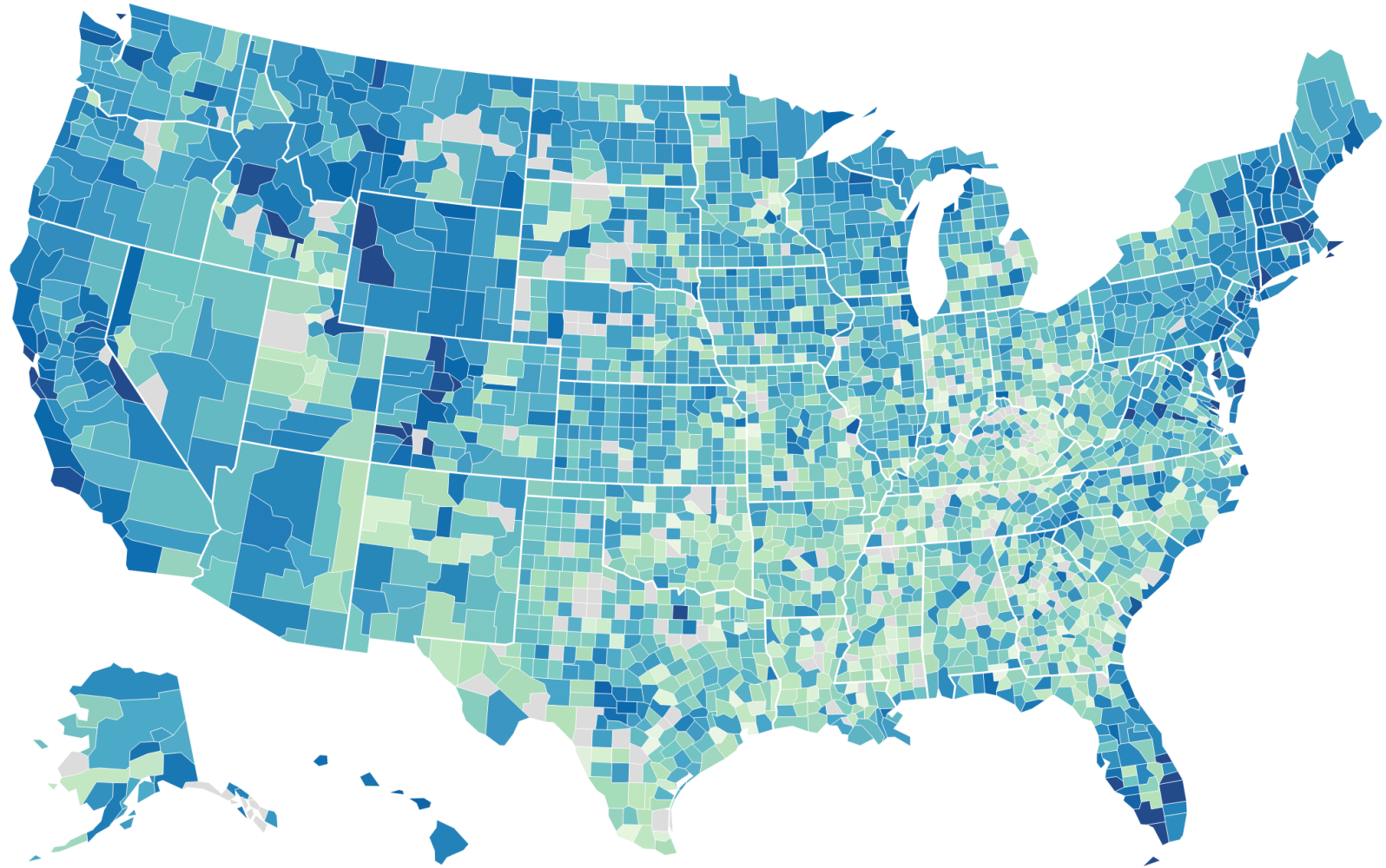
Definition: consumption

Definition: FWCP

Data: CountyPlus

Net Worth Per Capita (2006)

\$million



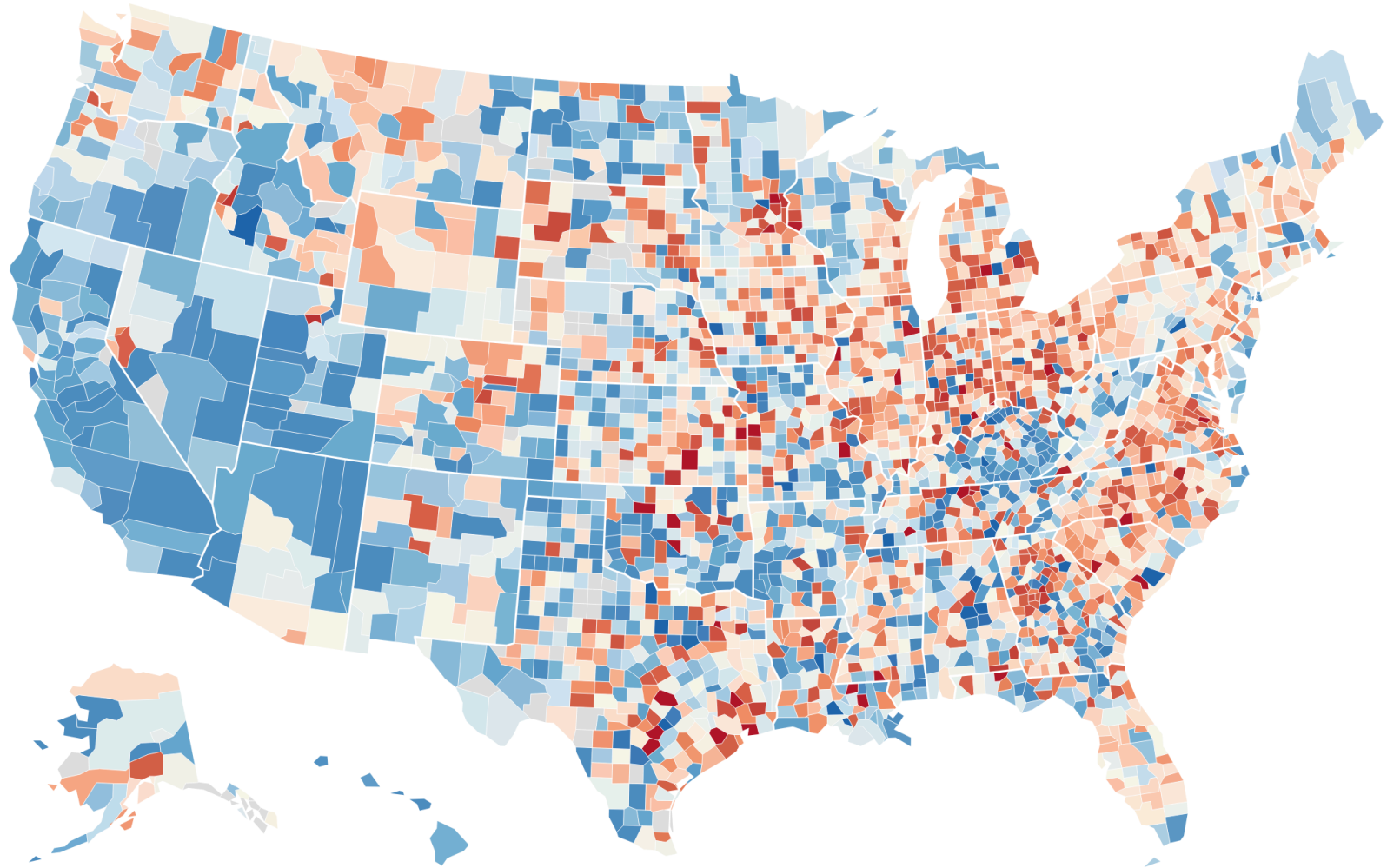
Source: CountyPlus • Created with Datawrapper

Figure 3: Geographical: Pre-crisis net worth

Data: CountyPlus

3-year Net Worth Shock (06-09)

(bottom & top 1% censored)



Source: CountyPlus • Created with Datawrapper

Figure 4: Geographical: Net worth shock during the Great Recession

Data: CountyPlus

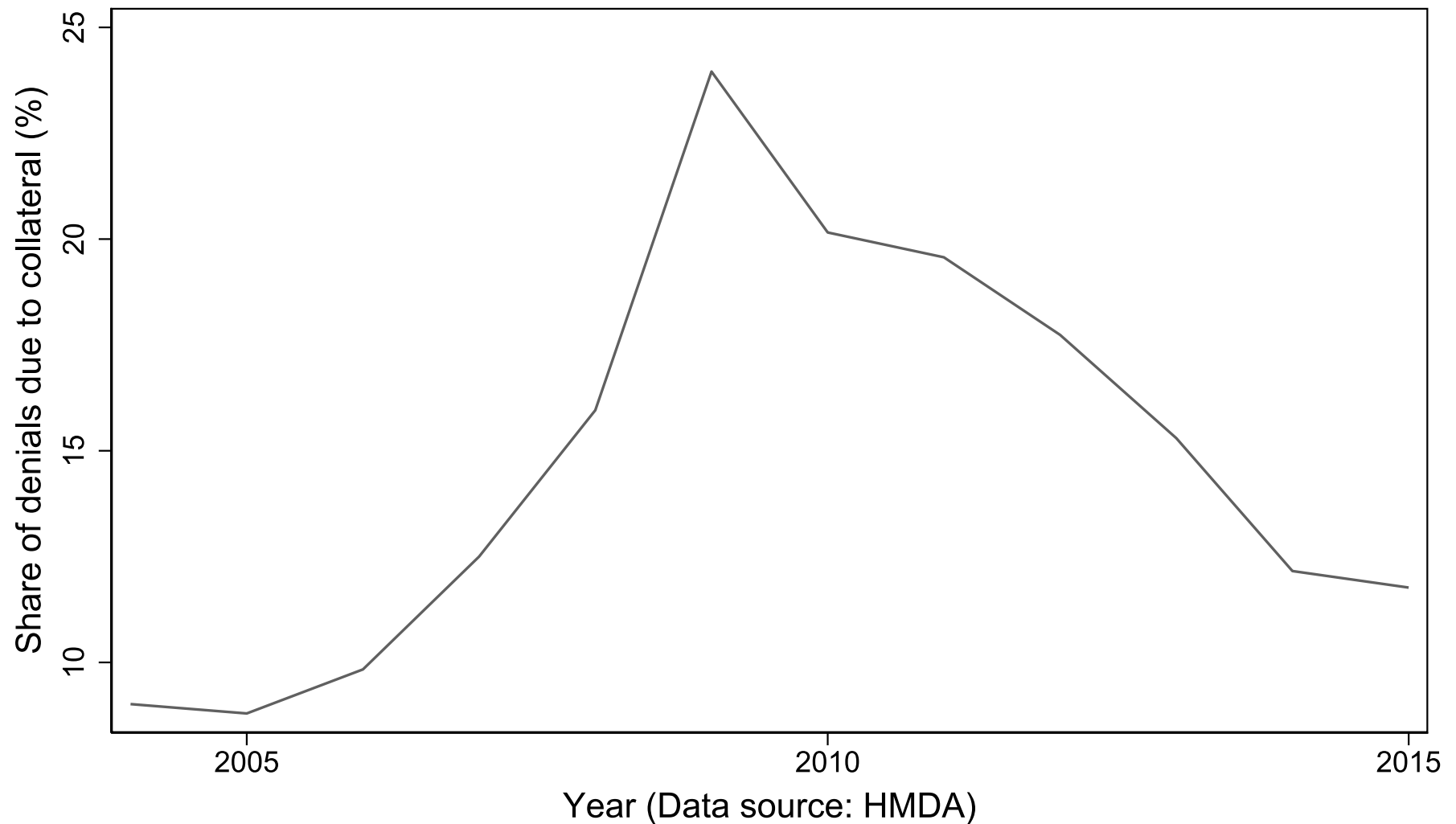


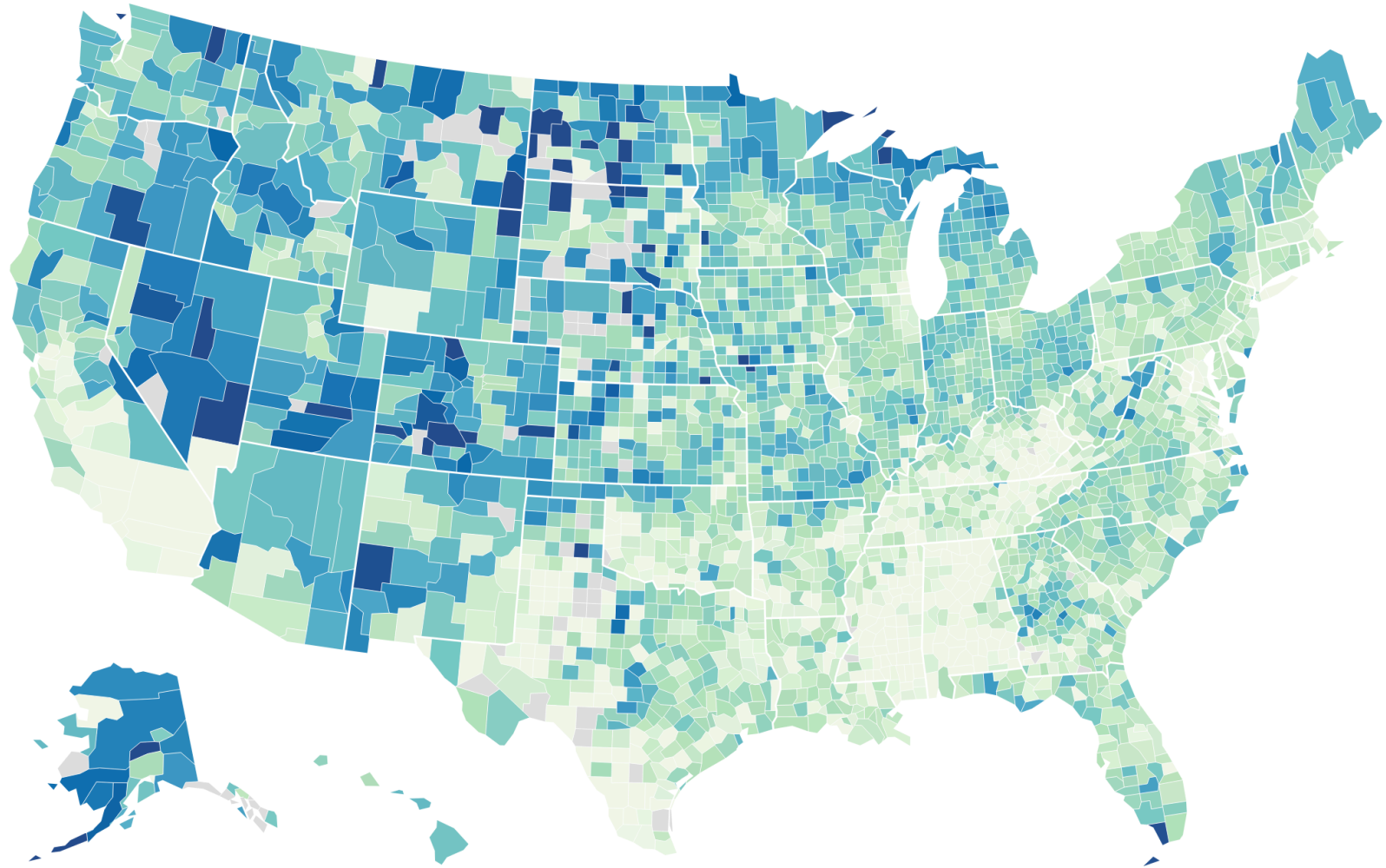
Figure 5: The aggregate extent of collateral constraint

- Larger *DENI*, larger friction

Data: CountyPlus

Home Mortgage Denial Share Due to Lack of Collateral

03-06 average



Source: CountyPlus • Created with Datawrapper

Figure 6: Geographical: Collateral constraint before the crisis

Data: CountyPlus

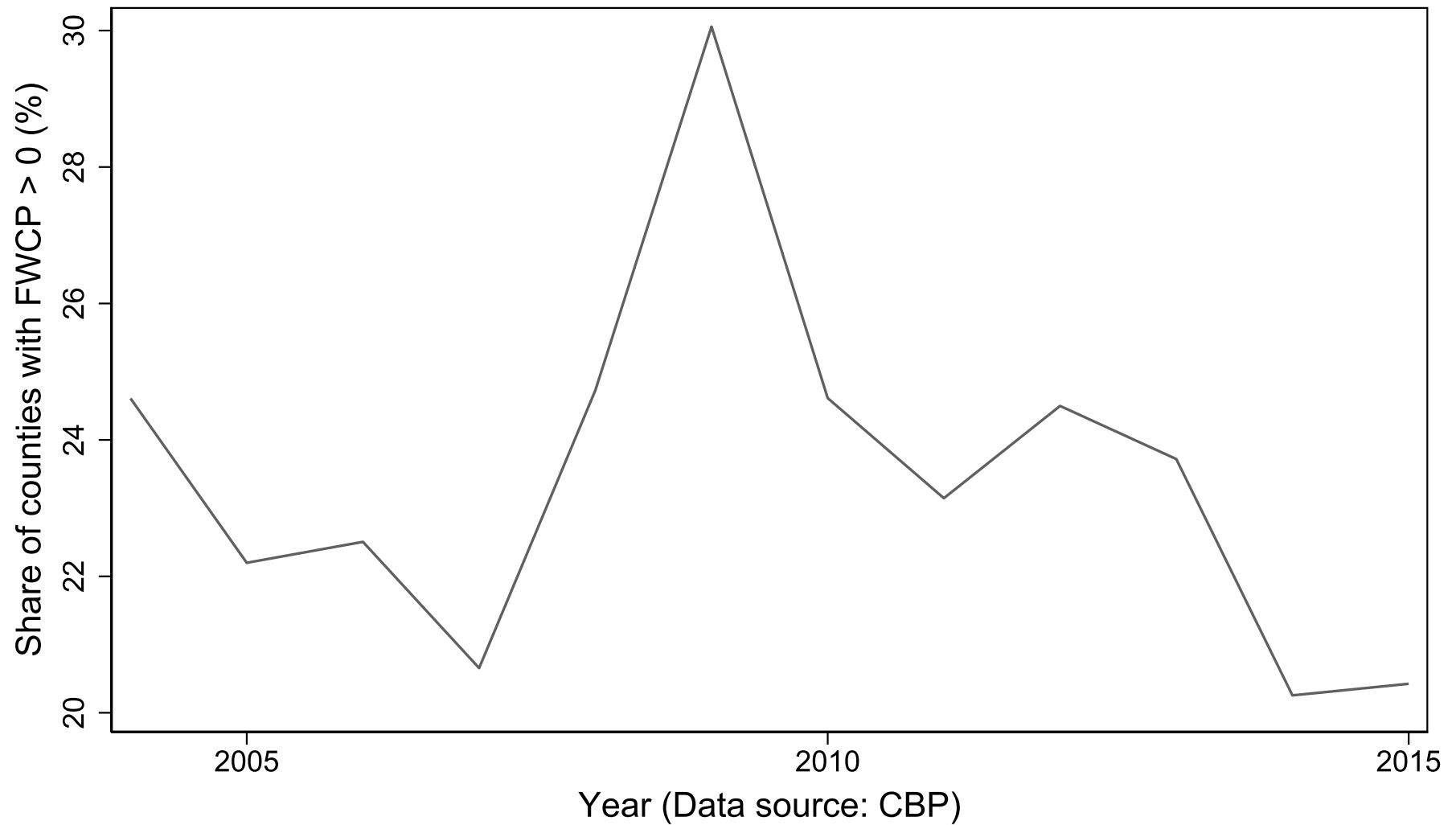


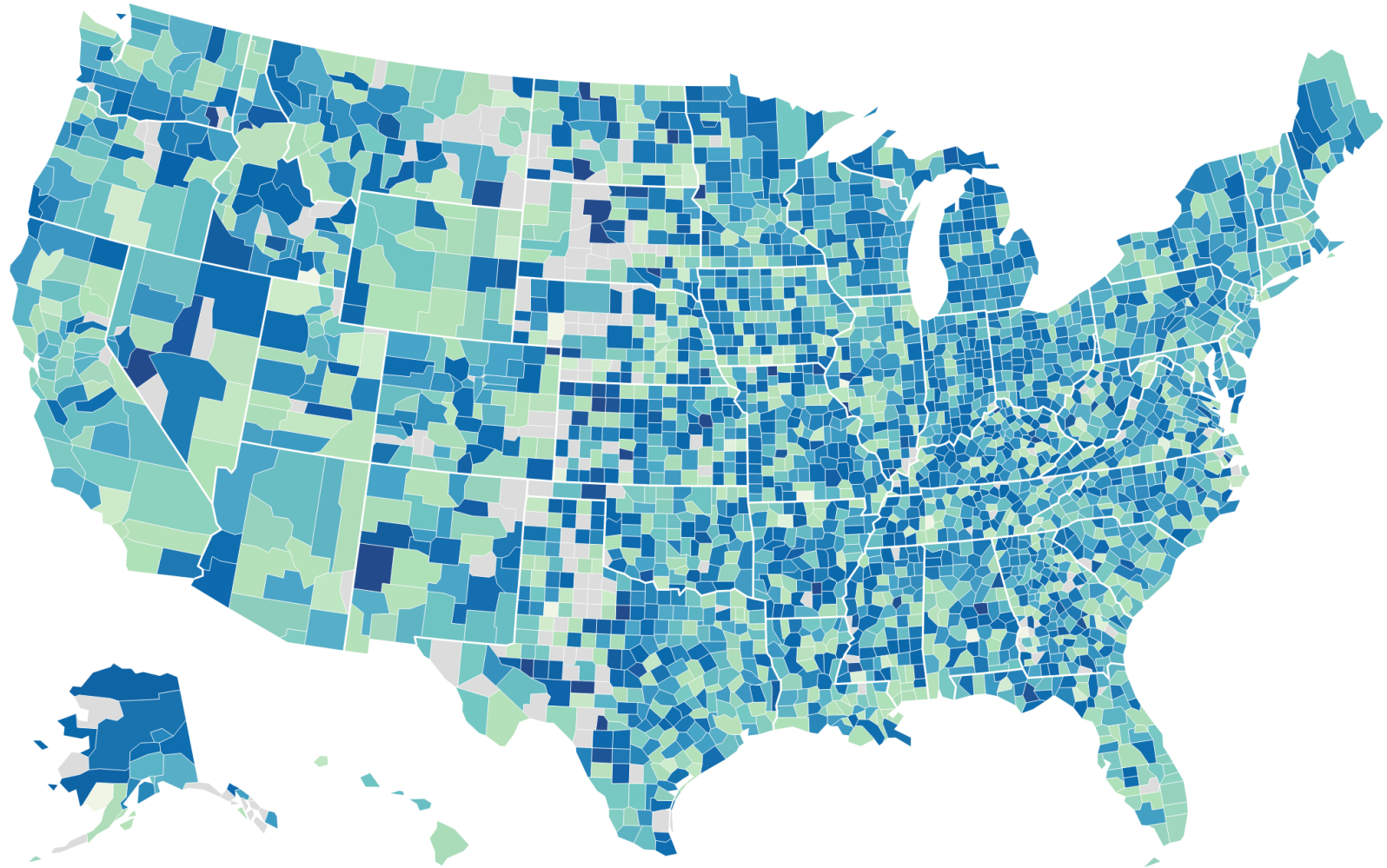
Figure 7: The aggregate extent of DNWR

- Larger *DNWR*, larger friction

Data: CountyPlus

Fraction of Wage Cuts Prevented

(03-06 average)



Source: CountyPlus • Created with Datawrapper

Figure 8: Geographical: DNWR before the crisis

Data: CountyPlus

Compare with the aggregate series:

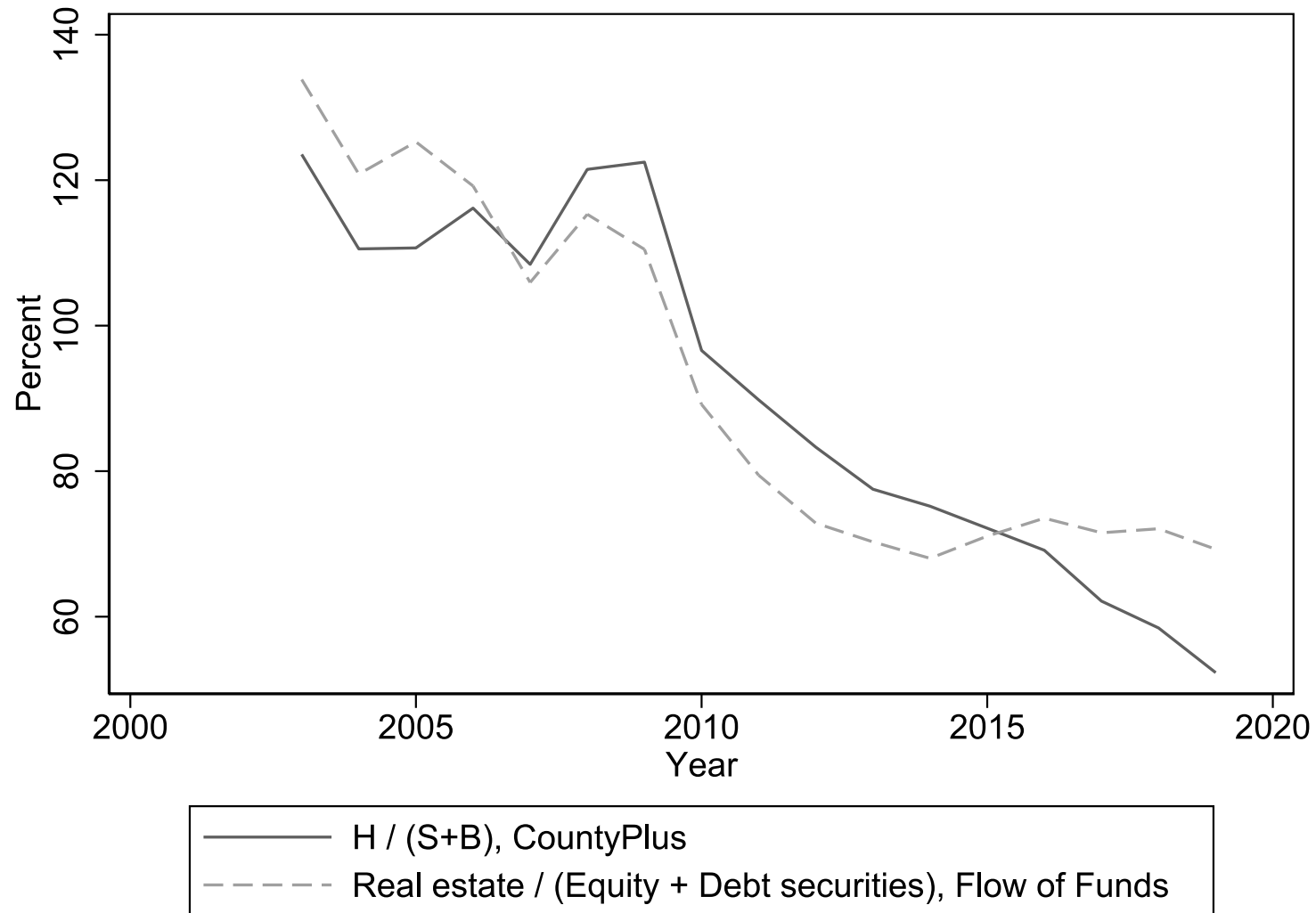


Figure 9: CountyPlus vs. Fed Flow of Funds

Baseline specification

A semi-varying coefficient variant of the linear LP in [Cloyne, Jordà and Taylor \(2023\)](#)

$$y_{i,t+h} = \alpha_h + x_{i,t} \cdot \beta_h(\Delta \mathbf{Z}_{i,t}) + \Delta \mathbf{Z}'_{i,t} \boldsymbol{\delta}_h + g(N_{i,t-1}) + \mathbf{W}_{i,t} \boldsymbol{\lambda}_h + \iota_{i \in s} + \nu_t + \varepsilon_{i,t+h}$$

• where

- $\Delta \mathbf{Z}_{i,t}$: *DENI* and *FWCP* deviation from the county's mean level
- $\beta_h(\Delta \mathbf{Z}_{i,t})$: effects of the net worth shock
- $h = 0, \dots, H$: projection horizons
- $y_{i,t+h}$: outcomes
- $g(N_{i,t-1})$: a functional control of lagged net worth
- $\iota_{i \in s}, \nu_t$: state and year fixed effects

• Sieve estimator of global polynomial approximation:

$$\beta_h(\Delta \mathbf{Z}_{i,t}) \approx b_h^0 + b_h^1 \Delta z_{i,t}^{fwcp} + b_h^2 \Delta z_{i,t}^{deni} + b_h^3 \Delta z_{i,t}^{fwcp} \Delta z_{i,t}^{deni} + b_h^4 (\Delta z_{i,t}^{fwcp})^2 + b_h^5 (\Delta z_{i,t}^{deni})^2$$

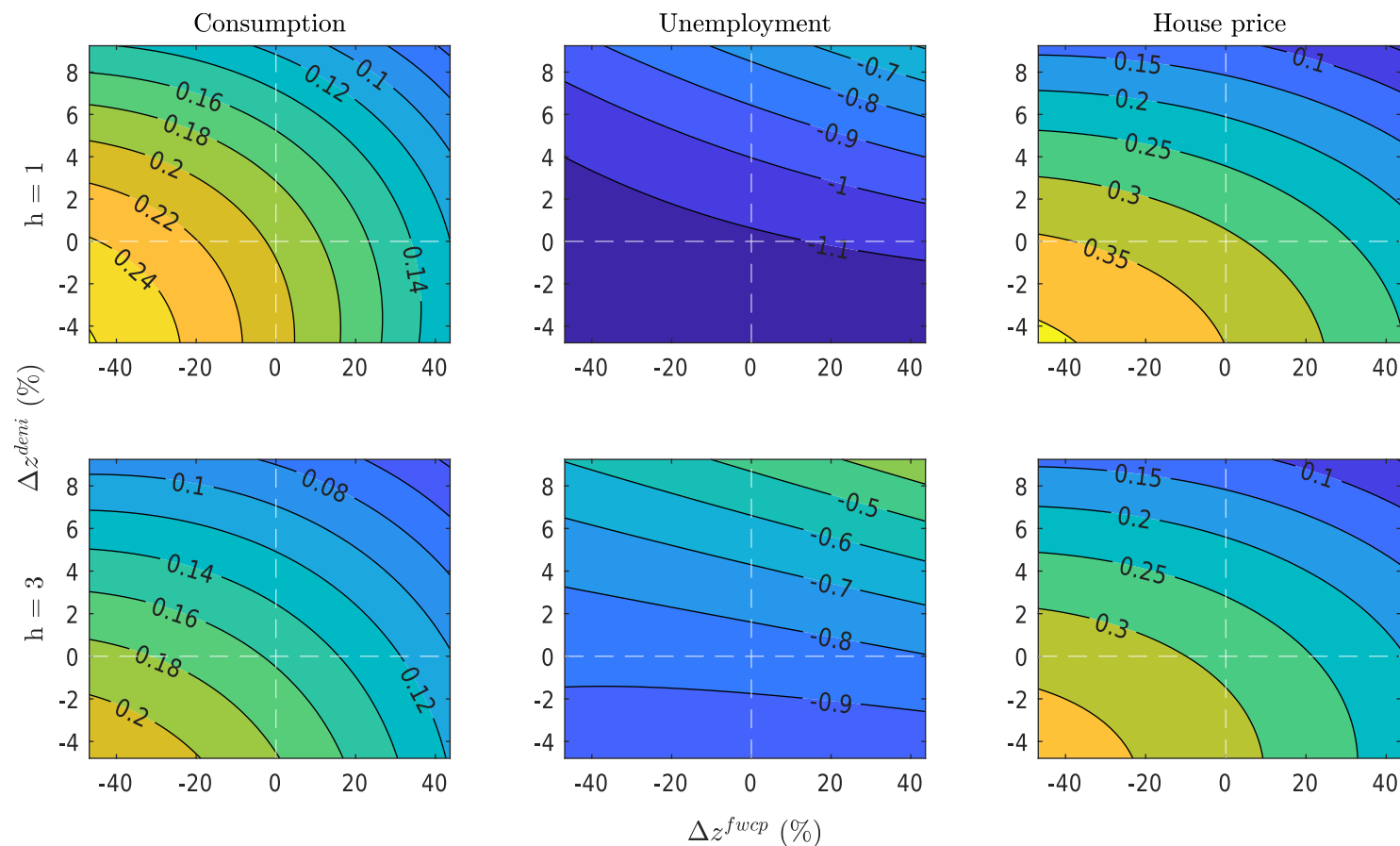
• Outcomes: Log real consumption per capita; Unemployment rate; Log real house price index

Page: robustness checks

Page: Controls

Baseline estimates of $\beta_h(\Delta Z)$

The estimated effect $\beta_h(\Delta Z)$ is 2-dimensional functions (+1% shock):

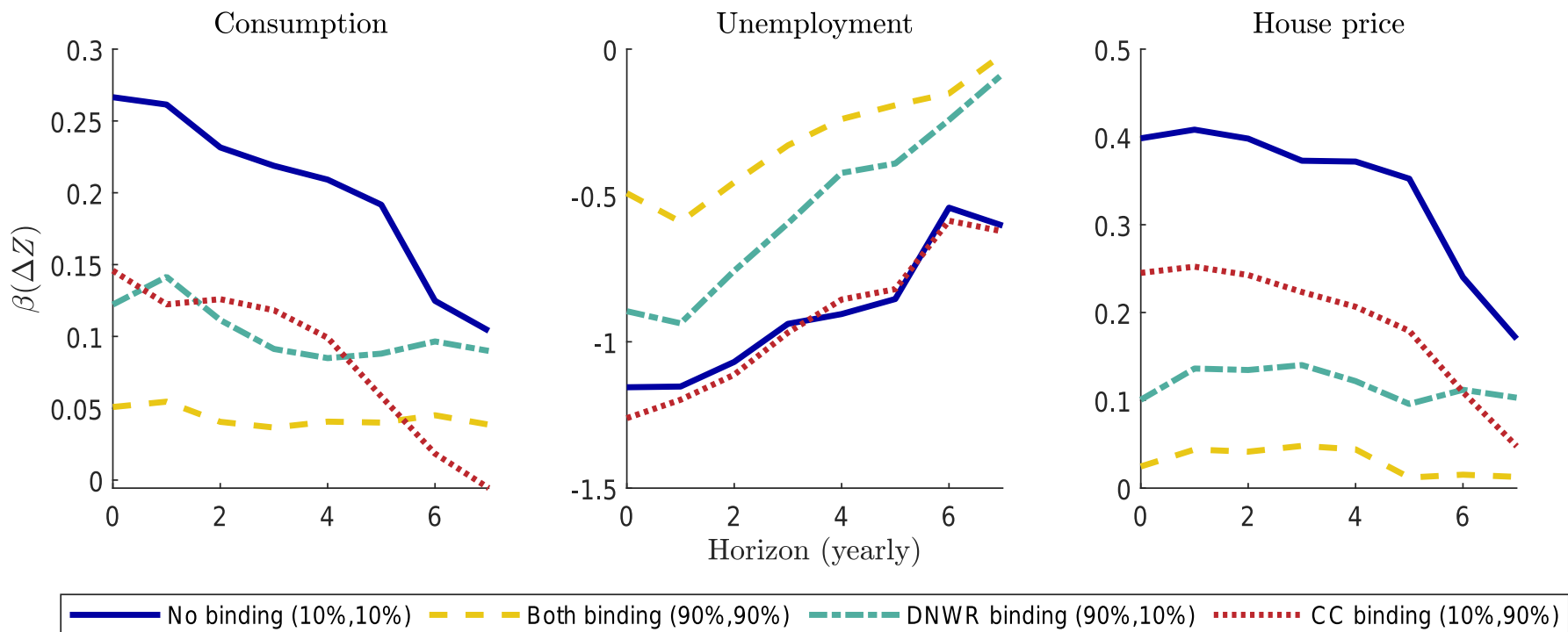


- Contour interval: heterogeneity of the effects
- Contour curvature: interaction & non-linearity

Other horizons

Baseline estimates of $\beta_h(\Delta Z)$

Counterfactual IRF by scenario:



Policy implication:

- Policies based on local economic conditions
- Policies to reduce local friction levels

Baseline vs. Linear LP

- Baseline specification

$$y_{i,t+h} = \alpha_h + x_{i,t} \cdot \beta_h(\Delta \mathbf{Z}_{i,t}) + \Delta \mathbf{Z}_{(i,t)}' \delta_h + g(N_{i,t-1}) + \mathbf{W}_{i,t} \lambda_h + \iota_{i \in s} + \nu_t + \varepsilon_{i,t+h}$$

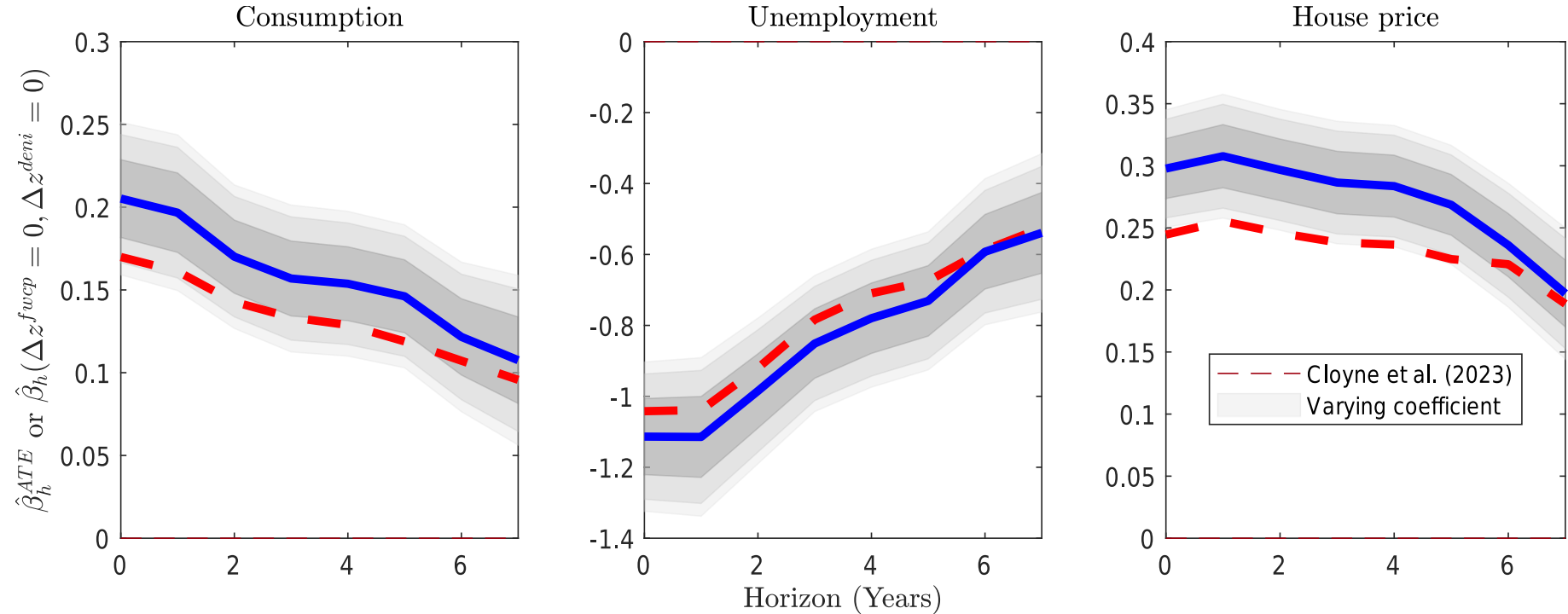
- Linear LP with linear heterogeneous effects [Cloyne, Jordà and Taylor \(2023\)](#)

$$y_{i,t+h} = \alpha_h + x_{i,t} \beta_h + x_{i,t} \Delta \mathbf{Z}'_{i,t} \begin{bmatrix} \gamma_h^{fwcp} \\ \gamma_h^{deni} \end{bmatrix} + \Delta \mathbf{Z}'_{i,t} \delta_h \\ + g(N_{i,t-1}) + \mathbf{W}_{i,t} \lambda_h + \iota_{i \in s} + \nu_t + \varepsilon_{i,t+h}, h = 0, \dots, H$$

where γ_h^{fwcp} and γ_h^{deni} are the linear heterogeneous effects

Baseline vs. Linear LP

Consistent estimates at the average county:

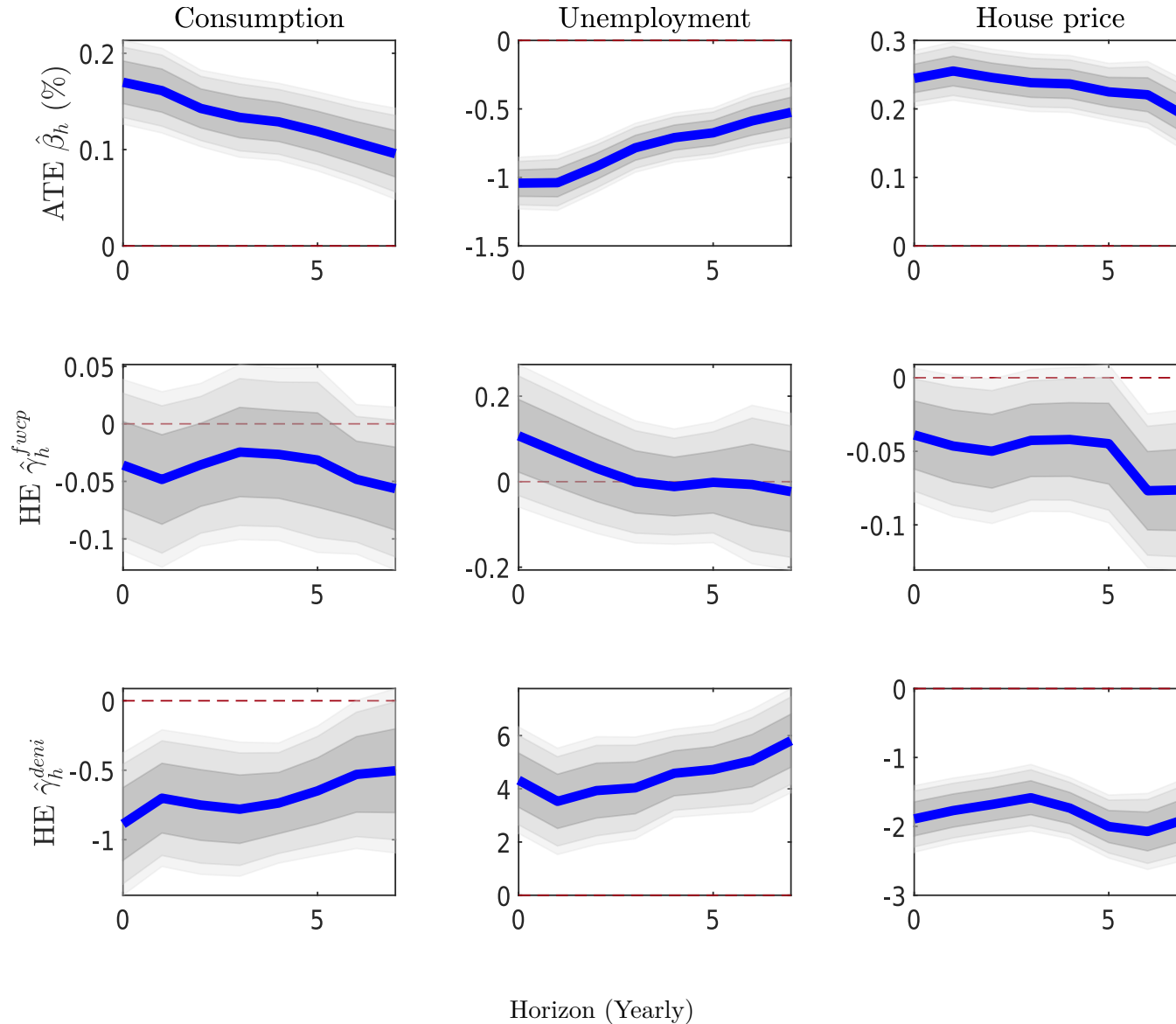


where

- Blue solid line: $\hat{\beta}_h(\Delta \mathbf{Z} = 0)$ of the baseline model
- Red dashed line: $\hat{\beta}_h$ of the linear LP model
- CI: 95%, 90%, 1- σ deviation

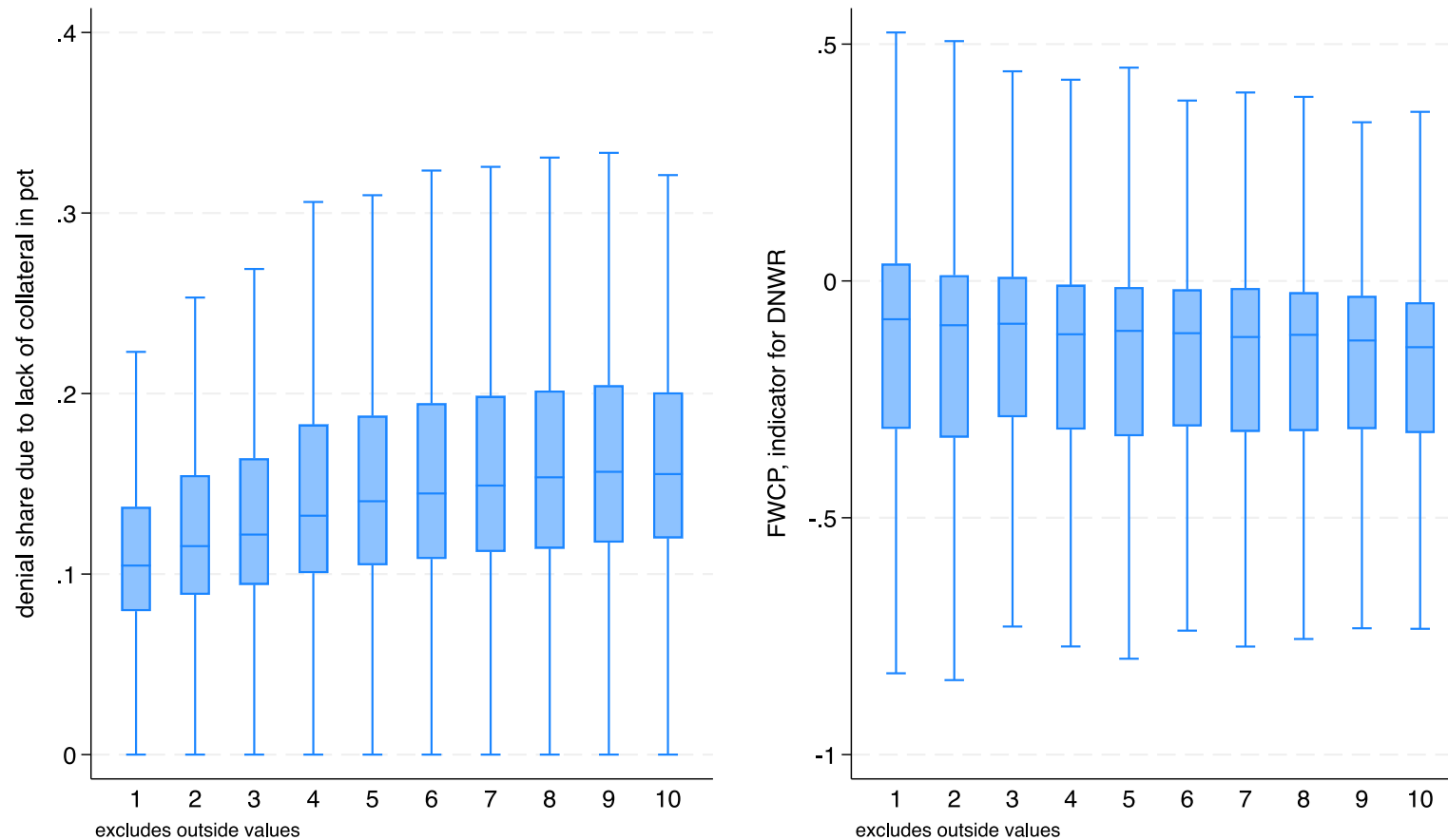
Baseline vs. Linear LP

The linear LP misses the heterogeneous effects of DNWR & friction interaction:



Heterogeneity among income groups

Counties with different income levels experiencing varying degree of frictions:



⇒ Important implications for the transmission of macroeconomic shocks and the design of stabilization policies

Heterogeneity among income groups

Check $\beta(\Delta Z = 0)$:



- Vulnerability against shock:

- Consumption: Low
- Unemployment: Low & Middle
- House price: Middle & Top

⇒ National policy may potentially exacerbate existing inequalities

⇒ Policies targeting at different outcomes in different regions of income

Inference

- F -test: non-linearity of heterogeneous effects and friction interaction

$$H_0 : 0 = b_h^3 = b_h^4 = b_h^5$$

Horizon	0	1	2	3	4	5	6	7
Consumption	8.403*** (.000)	8.641*** (.000)	6.127*** (.000)	5.289*** (.001)	5.627*** (.001)	7.282*** (.000)	5.286*** (.001)	4.002*** (.008)
Unemployment	5.919*** (.001)	3.874*** (.009)	2.551* (.054)	2.963** (.031)	3.453** (.016)	3.292** (.020)	2.532* (.056)	1.627 (.181)
House price	24.967*** (.000)	23.961*** (.000)	22.215*** (.000)	21.083*** (.000)	22.661*** (.000)	19.744*** (.000)	14.116*** (.000)	11.973*** (.000)

Notes: 1. Numbers in the parenthesis are the p -value. 3. ***: $p < 0.01$, **: $p < 0.05$, *: $p < 0.1$

- The F -test suggests significant non-linear heterogeneous effects and the interaction between collateral constraint and DNWR

Robustness

- **Order selection of the polynomial approximation** [Appendix](#)
 - Suggests higher order approximation not introduce new patterns
- **Sensitivity analysis against confounders** [Appendix](#)
 - Shows the baseline result is robust against potential confounders
- **Local estimator** [Appendix](#)
 - Shows the same patterns of $\beta_h(\Delta Z)$
- **Profile-likelihood ratio test** [Appendix](#)
 - Rejects H_0 as well
- **Geographical spillover effects of the shock** [Appendix](#)
 - Finds statistically significant spillover effects of the shocks on unemployment \implies larger non-linearity

[Goto: Specification](#)

Conclusion

- **Findings**

- Economic frictions greatly shape the effect of net worth shocks in which collateral constraints and DNWR and their interaction could explain the US recovery after the Great Recession
- There are large non-linear heterogeneous effects of net worth shocks in the US which bring important policy implications

- **Policy implications**

- Call for policies advocating for a strong labor market and mitigating financial risks
- Call for policies based on local economic conditions
- Country-wise interventions may have uneven effects across the income distribution, potentially worsening existing inequalities

End

Thank you!

Latest version available at SSRN ID: [4915272](https://ssrn.com/abstract/4915272)

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Appendix: Other horizon of the baseline

$\beta_h(\Delta Z)$ at horizon $h = 5, 7$

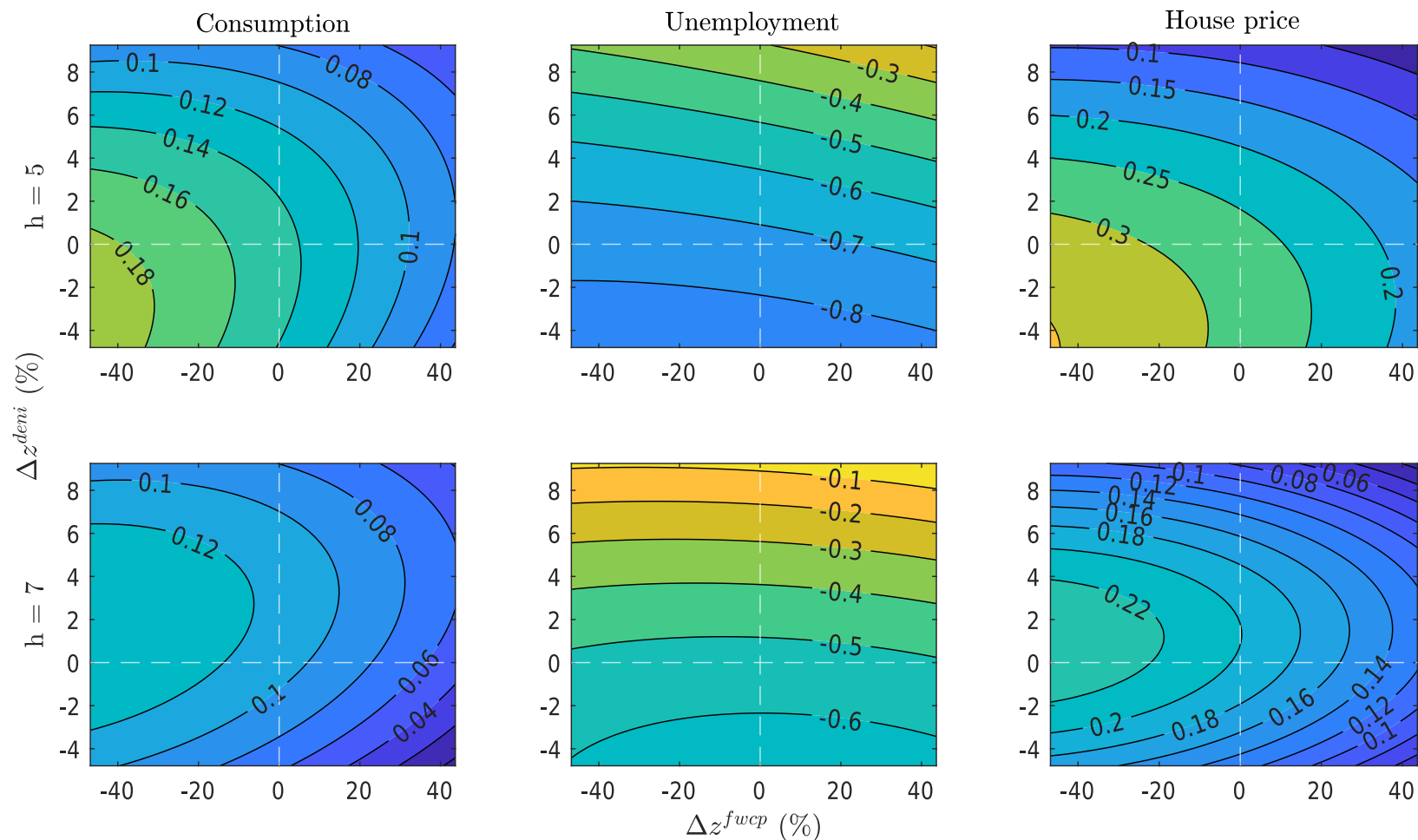


Figure 15: $\beta_h(\Delta Z)$

Goto: baseline

Appendix: variable definitions

- Household **net worth** of county i in year t :

$$NW_{it} = S_{it} + B_{it} + H_{it} - D_{it}$$

where S is equity, B is debt security, H is housing wealth, and D is debt

- Equity** and **Debt security holding**:

$$S_{i,t} = \frac{\text{County dividend income}_{i,t}}{\sum_j \text{County dividend income}_{j,t}} \times \text{National total equity of household}_t$$

$$B_{i,t} = \frac{\text{County interest income}_{i,t}}{\sum_j \text{County interest income}_{j,t}} \times \text{National total debt security of household}_t$$

- Data sources of S and B : Survey of Income (SOI) by IRS, Fed Flow of Funds

Appendix: variable definitions

- **Debt:**

$$D_{i,t} = \text{Household debt-to-income ratio}_{i,t} \times \text{AGI}_{i,t}$$

where i is county index and t is year index, AGI is adjusted gross income.

- **Housing wealth**

$$H_{i,t} = \frac{\text{Total housing units}_{i,t}}{\text{Average housing units per house}} \times \text{Median house value}_{i,2019} \times \frac{\text{HPI}_{i,t}}{\text{HPI}_{i,2019}}$$

where the average housing units per house is 1.8

- Data sources of D and H : SOI; Enhanced Financial Account of Fed Flow of Funds; Census Bureau; American Community Survey (ACS); Federal Housing Finance Agency (FHFA)

[Goto: Data](#)

Appendix: variable definitions

- Spirit of [Zhou and Carroll \(2012\)](#): tax data
- Sales tax data from local department of revenues: 27 states, 1700 counties

$$C_{i,t} = \text{PCE}_{s,t} \times \text{Population}_{s,t} \times \frac{\text{Taxable sales}_{i,t}}{\sum_{j \in s} \text{Taxable sales}_{j,t}}$$

- Currently available states (sorted by FIPS code):

1 Alabama, 4 Arizona, 5 Arkansas, 6 California, 8 Colorado, 12 Florida, 17 Illinois, 18 Indiana, 19 Iowa, 22 Louisiana, 27 Minnesota, 29 Missouri, 31 Nebraska, 32 Nevada, 36 New York, 37 North Carolina, 38 North Dakota, 39 Ohio, 42 Pennsylvania, 45 South Carolina, 47 Tennessee, 49 Utah, 50 Vermont, 51 Virginia, 55 Wisconsin, 56 Wyoming.

Appendix: variable definitions

- Some states only report tax revenue \implies measurement error due to differential tax rate
- Year t , county i , total J types of goods; True consumption: $C_{j,i,t}$, tax revenue $T_{j,i,t}$, tax rate $\tau_{j,t}$
- True consumption distribution:

$$\tilde{S}_{i,t} := \frac{C_{i,t}}{\sum_{m=1}^I C_{m,t}} = \frac{\sum_{j=1}^J C_{j,i,t}}{\sum_{m=1}^I \sum_{j=1}^J C_{j,m,t}}$$

- Estimates:

$$S_{i,t} := \frac{T_{i,t}}{\sum_{m=1}^I T_{m,t}} = \frac{\sum_{j=1}^J C_{j,i,t} \tau_{j,t}}{\sum_{m=1}^I \sum_{j=1}^J C_{j,m,t} \tau_{j,t}}$$

- Measurement error:

$$S_{i,t} = \frac{\bar{\tau}_{i,t} \sum_{j=1}^J C_{j,i,t}}{\bar{\tau}_t \sum_{m=1}^I \sum_{j=1}^J C_{j,m,t}} = \frac{\bar{\tau}_{i,t}}{\bar{\tau}_t} \tilde{S}_{i,t}$$

where:

$$\bar{\tau}_{i,t} = \frac{\sum_{j=1}^J C_{j,i,t} \tau_{j,t}}{\sum_{j=1}^J C_{j,i,t}} \quad \bar{\tau}_t = \frac{\sum_{m=1}^I \sum_{j=1}^J C_{j,m,t} \tau_{j,t}}{\sum_{m=1}^I \sum_{j=1}^J C_{j,m,t}}$$

are county & state average tax rates

[Goto: Data](#)

Appendix: variable definitions

- Methodology of [Holden and Wulfsberg \(2009\)](#)
- **Idea:** true nominal wage distribution vs. constructed notional rigidity-free distribution
- Notional distribution: all county-industry pairs with upper 25% wage growth in a given year
- Fraction of Wage Cuts Prevented:

$$\text{FWCP}_{i,t} = 1 - p_{i,t}/\tilde{p}_{i,t}$$

$$\tilde{p}_{i,t} := \frac{\#\{Z_{i,t} < 0\}}{N_t^{\text{top 25\%}}}$$

$$p_{i,t} := \frac{\#\{\Delta w_{j,i,t} < 0\}}{N_{i,t}}$$

where $Z_{i,t}$ is the rigidity-free wage growth from the notional distribution of county i in year t ; $\Delta w_{j,i,t}$ is the true wage growth of industry j

[Goto: Data](#)

Appendix: Illustration parameters

Parameter	Definition	Value
β	Utility discounting factor	0.9
α	Labor income share	0.7
δ	Parameter of DNWR	0.99
θ	Collateral constraint as LTV ratio	0.8
A	Technology level	1
$\bar{\nu}$	Steady state LTV ratio	0.79
γ	Housing preference	0.8
H	House supply	30

Goto: comparative statistics

Appendix: Sensitivity analysis

- Framework of [Cinelli and Hazlett \(2020\)](#)
- If there are confounder(s), how strong must it be explaining the residual to:
 - Flip the coefficient sign
 - Overturn the t -tests
- e.g. Policy intervention not captured by fixed effects
- Scalar measures and **contour figures** regarding:
 - $R_{D \sim Z, X}^2$: partial R^2 of confounder(s) Z wrt treatment D
 - $R_{Y \sim Z | D, X}^2$: partial R^2 of confounder(s) Z wrt outcome Y
- Benchmark variable: what if confounder(s) are as strong as an a specific existing regressor?

Goto: Robustness

Appendix: Sensitivity analysis

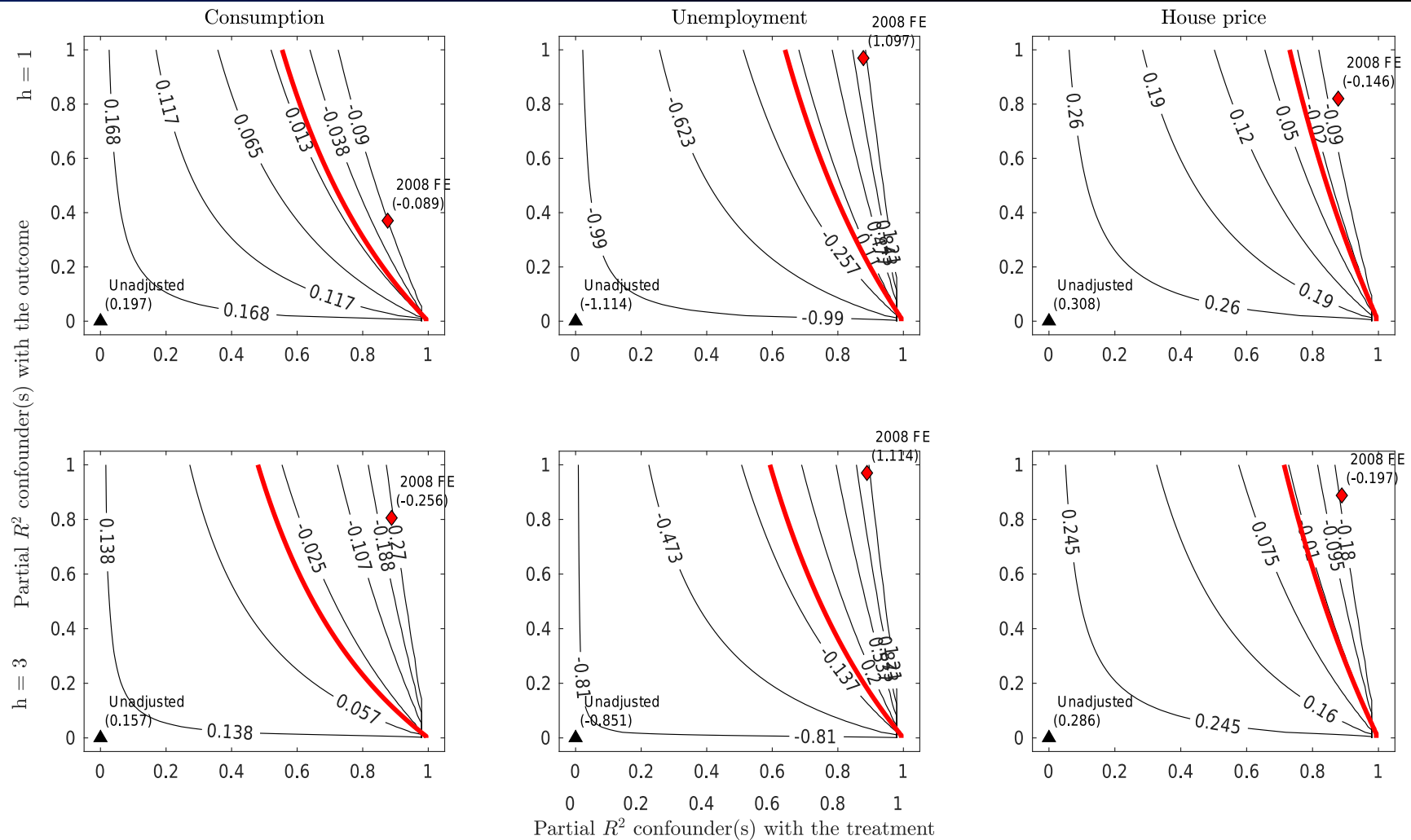


Figure 16: Point estimate of $\beta_h(\Delta Z = 0)$

where the **red** line marks zero (threshold of sign flip)

- Benchmarking: 2008 year fixed effects

Appendix: Sensitivity analysis

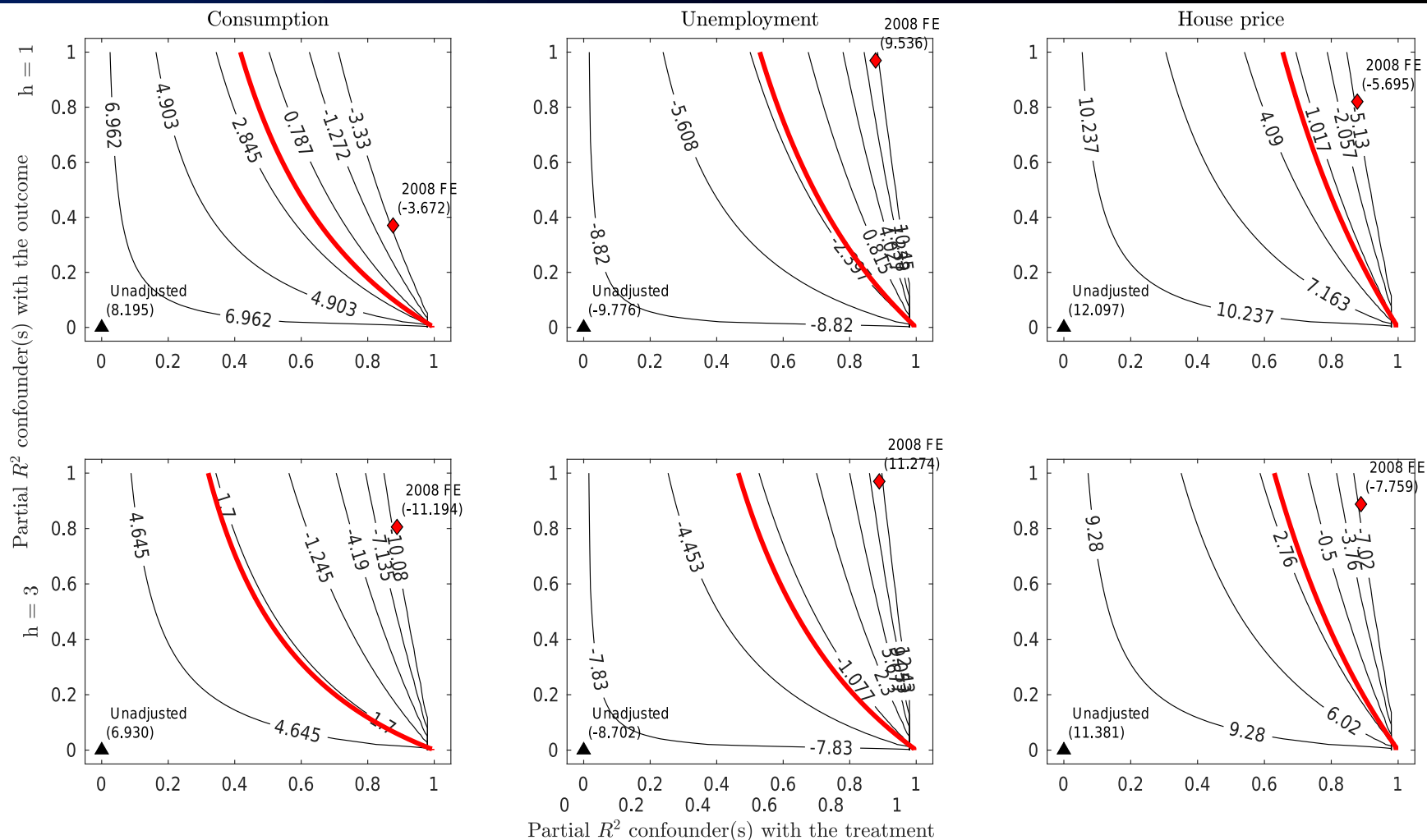


Figure 17: t -statistic of $\beta_h(\Delta Z = 0)$

where the red line marks $\alpha = 5\%$ criteria value of t -test

- Benchmarking: 2008 year fixed effects

Appendix: Order selection

Expanding $\beta_h(\Delta Z)$ to the 3rd order:

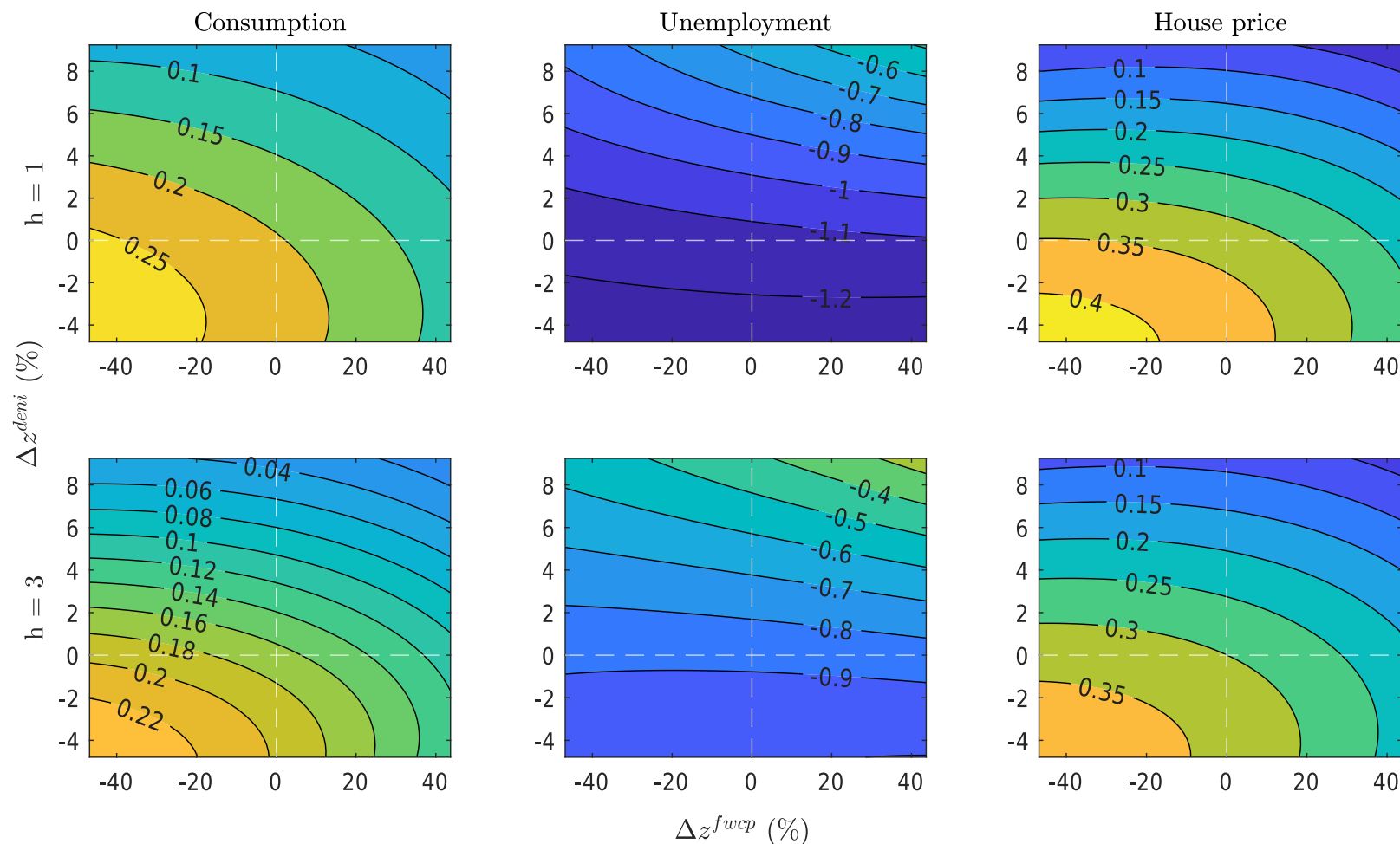


Figure 18: $\beta_h(\Delta Z)$

Goto: baseline

Appendix: Local linear estimator

- Global polynomial may mask important local features \implies check local estimators
- Use local linear estimator:
 - Gaussian kernel for $\Delta \mathbf{Z}$, Normalized Euclidean distance
 - 17×17 quantile knots in percentage range $[10\%, 90\%]^2$ (every 5%)
 - Two-step estimation procedure in [Zhang, Lee and Song \(2002\)](#)
 - Plug-in bandwidth estimator in [Yang and Tschernig \(1999\)](#)

Appendix: Local linear estimator

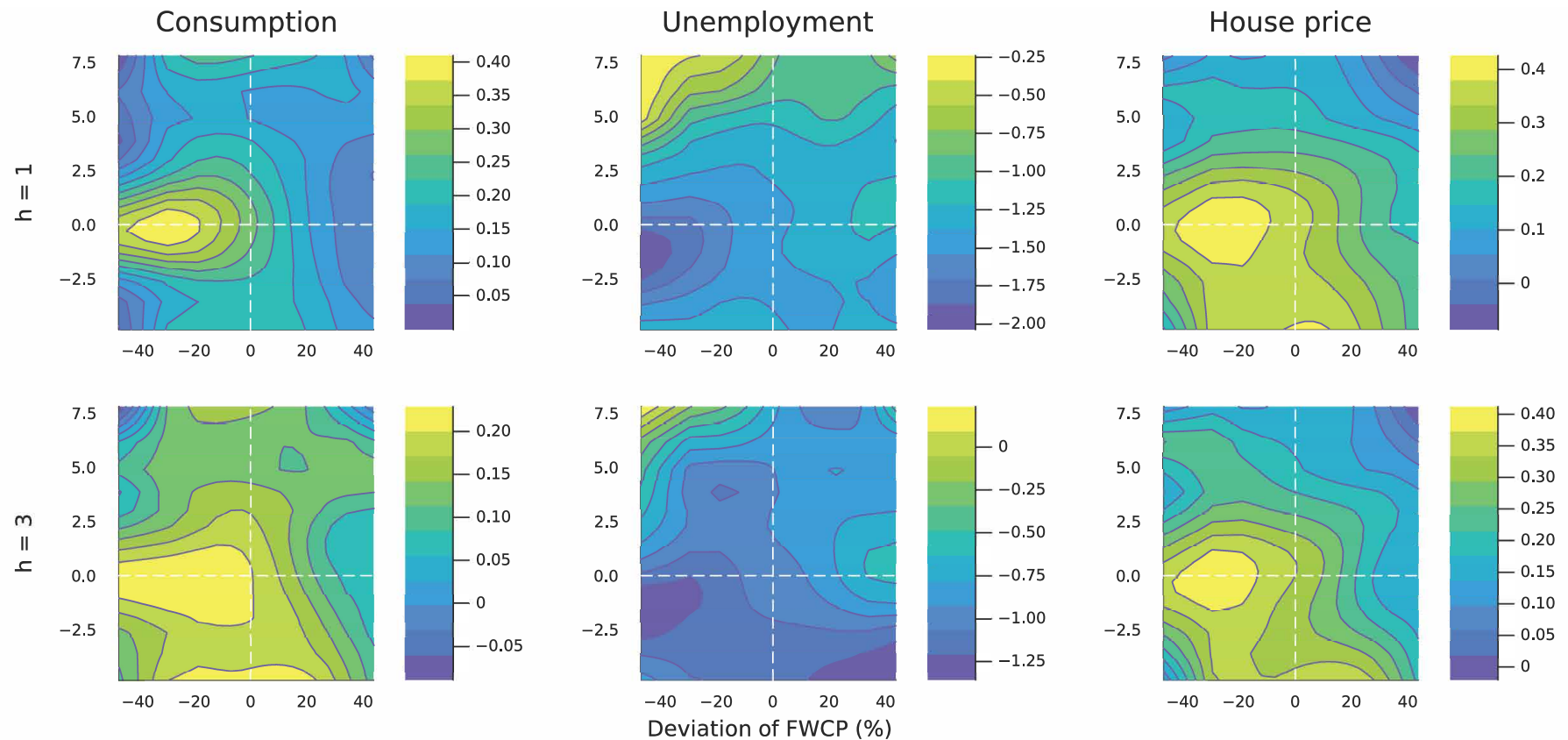


Figure 19: $\beta_h(\Delta Z)$

- No significant new features cp. baseline

Goto: robustness

Appendix: Profile-likelihood ratio (PLR) test

- The F -test depends on the parametric assumption of the global polynomial
 \implies PLR test by [Fan and Huang \(2005\)](#) which test $\beta_h(\Delta Z)$ as a whole
- H_0 : if the overall treatment effect β_h is dependent on Δz^{fwcp} and Δz^{deni} and the baseline model is correctly specified, then it equals to the estimates from the linear LP model

Goto: Robustness

- Table (next page):

Appendix: Profile-likelihood ratio (PLR) test

Horizon	Consumption	Unemployment	House price
0	3230.96*** (0.1503)	328.46*** (0.1503)	1596.15*** (0.1503)
1	2921.63*** (0.1504)	355.91*** (0.1504)	1166.61*** (0.1504)
2	3345.83*** (0.1504)	1301.31*** (0.1504)	1230.62*** (0.1504)
3	3069.98*** (0.1504)	1684.84*** (0.1504)	1127.61*** (0.1504)
4	2615.89*** (0.1504)	1605.61*** (0.1504)	589.91*** (0.1504)
5	2264.8*** (0.1503)	1829.66*** (0.1504)	770.64*** (0.1504)
6	1886.03*** (0.1503)	1837.51*** (0.1503)	841.8*** (0.1503)
7	1630.81*** (0.1502)	1799.62*** (0.1502)	935.84*** (0.1502)

where the number with stars are the generalized likelihood ratio statistic T_0 , the number in parenthesis is δ_n the degree of freedom of the asymptotic $\chi_{\delta_n}^2$ distribution, the other asymptotic parameter $r_K \approx 0.51579$ for our Gaussian kernel.

Appendix: Spatial spillover effects

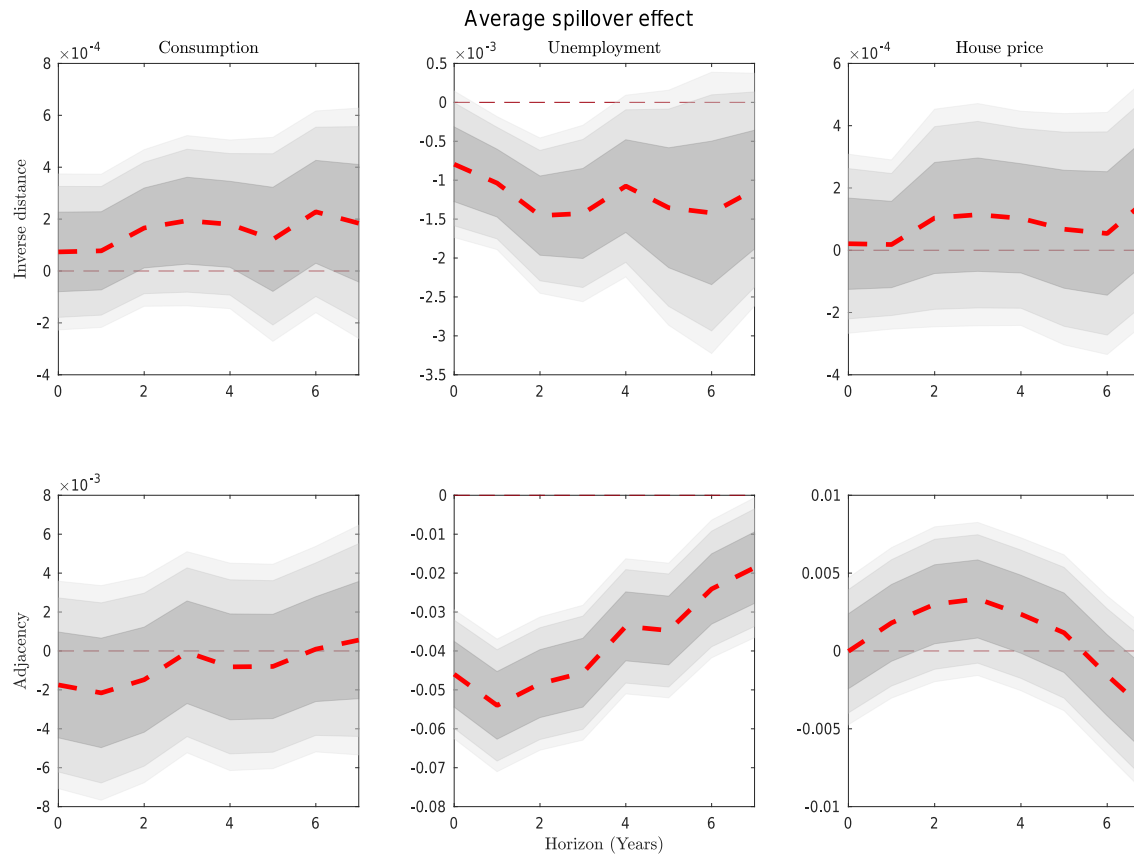
- Neighboring counties may share markets (e.g. labor market of a metropolitan) \implies spillover effects of net worth shocks
- Re-estimate the baseline model but:
 - adding a spatial Durbin term: $\eta_h \cdot \mathbf{W} \mathbf{X}_t$
 - assuming no spillover effects of the outcomes and error

where \mathbf{W} is spatial weighted matrix, \mathbf{X}_t is stacked net worth shock in year t , and η_h is the coefficient of average spillover effect

- In this special case of Spatial Durbin model, the average indirect/spillover effect defined by [LeSage and Pace \(2009\)](#) degenerates to a number constantly proportional to η_h
- We test two types of spatial weight matrices:
 - Inverse distance weighting
 - 1st-closest neighbor adjacency weighting

Appendix: Spatial spillover effects

Average spillover effect η_h :



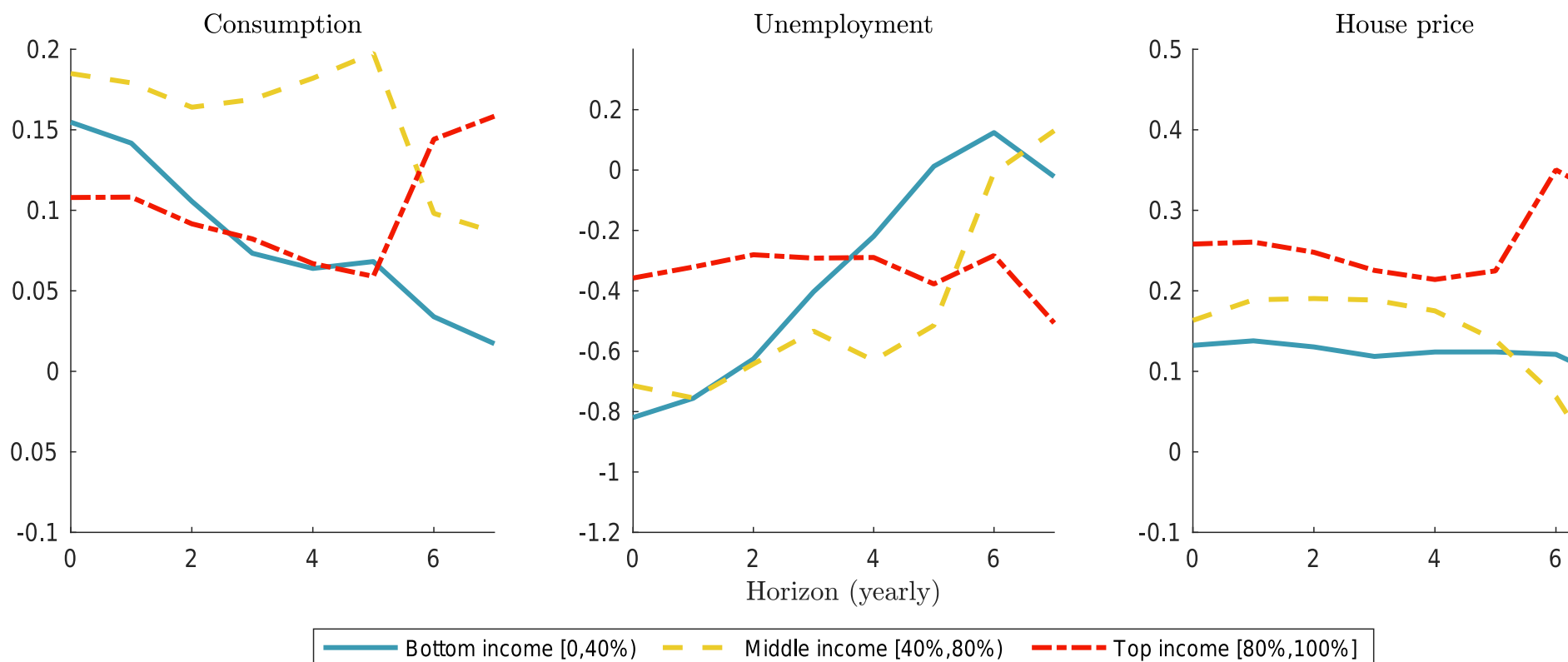
- Significant spillover effect of the shock on local labor markets
- Does not change $\beta_h(\Delta Z)$ in the other ΔZ areas except the “top-right” corner \implies even larger non-linearity

Goto: Robustness

Appendix: Counterfactual IRF among income groups

Scenario: Neither binding (10%, 10%):

$$qt(\Delta FWCP, \Delta DENI) = (10\%, 10\%)$$



- Similar effect size among income groups

Appendix: Other details in the baseline model

Controls:

- $W_{i,t}$: Similar to [Mian, Rao and Sufi \(2013\)](#)
 - Total housing units
 - Share of housing wealth in household net worth
 - Share of tradable sector employment in total employment
 - Share of construction sector employment in total employment
- $g(N_{i,t-1})$: 3rd order polynomial approximation; controlling pre-determined economic conditions

Sample: 2004-2019; 1700 counties with consumption data available

Weights: county population

SE Cluster: state level

[Goto: baseline](#)

Bibliography

Bibliography

Bocola, L. and Lorenzoni, G. (2020) *Risk sharing externalities*

Christiano, L. J., Eichenbaum, M. S. and Trabandt, M. (2015) “Understanding the great recession,” *American Economic Journal: Macroeconomics*, 7(1), pp. 110–167

Cinelli, C. and Hazlett, C. (2020) “Making sense of sensitivity: Extending omitted variable bias,” *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 82(1), pp. 39–67

Cloyne, J., Jordà, Ò. and Taylor, A. M. (2023) *State-dependent local projections: Understanding impulse response heterogeneity*

Fan, J. and Huang, T. (2005) “Profile likelihood inferences on semiparametric varying-coefficient partially linear models,” *Bernoulli*, 11(6), pp. 1031–1057

Fan, J., Zhang, C. and Zhang, J. (2001) “Generalized likelihood ratio statistics and Wilks phenomenon,” *The Annals of statistics*, 29(1), pp. 153–193

Guerrieri, V., Lorenzoni, G. and Prato, M. (2020) “Schumpeter lecture 2019: Slow household deleveraging,” *Journal of the European Economic Association*, 18(6), pp. 2755–2775

Bibliography

- Holden, S. and Wulfsberg, F. (2009) “How strong is the macroeconomic case for downward real wage rigidity?,” *Journal of monetary Economics*, 56(4), pp. 605–615
- Hu, J. (2024) *Uniform inference on functional coefficients quantile regression model with endogeneity and its application*
- Jordà, Ò. (2005) “Estimation and inference of impulse responses by local projections,” *American economic review*, 95(1), pp. 161–182
- Jordà, Ò., Schularick, M. and Taylor, A. M. (2020) “The effects of quasi-random monetary experiments,” *Journal of Monetary Economics*, 112, pp. 22–40
- Kaplan, Greg, Mitman, Kurt and Violante, Giovanni L. (2020) “Non-durable consumption and housing net worth in the great recession: Evidence from easily accessible data,” *Journal of Public Economics*, 189, p. 104176–104177
- Kaplan, Greg, Mitman, Kurt and Violante, Giovanni L. (2020) “The housing boom and bust: Model meets evidence,” *Journal of Political Economy*, 128(9), pp. 3285–3345
- LeSage, J. and Pace, R. K. (2009) *Introduction to spatial econometrics*. Chapman, Hall/CRC
- Mian, A. and Sufi, A. (2014) “What explains the 2007–2009 drop in employment?,” *Econometrica*, 82(6), pp. 2197–2223

Bibliography

Mian, A., Rao, K. and Sufi, A. (2013) “Household balance sheets, consumption, and the economic slump,” *The Quarterly Journal of Economics*, 128(4), pp. 1687–1726

Schmitt-Grohé, S. and Uribe, M. (2016) “Downward nominal wage rigidity, currency pegs, and involuntary unemployment,” *Journal of Political Economy*, 124(5), pp. 1466–1514

Shen, W. and Yang, S.-C. S. (2018) “Downward nominal wage rigidity and state-dependent government spending multipliers,” *Journal of Monetary Economics*, 98, pp. 11–26

Yang, L. and Tschernig, R. (1999) “Multivariate bandwidth selection for local linear regression,” *Journal of the Royal Statistical Society Series B: Statistical Methodology*, 61(4), pp. 793–815

Zhang, W., Lee, S.-Y. and Song, X. (2002) “Local polynomial fitting in semivarying coefficient model,” *Journal of Multivariate Analysis*, 82(1), pp. 166–188

Zhou, X. and Carroll, C. D. (2012) “Dynamics of wealth and consumption: new and improved measures for US states,” *The BE Journal of Macroeconomics*, 12(2)